Definitions of Philosophical Terms

Michael H. Birnbaum

Kinds of Statements

<u>Definition</u>: A definition is a statement of equivalence. A definition permits us to use one term to refer to an object or concept that would require many. Definitions are neither true nor false, but it can be confusing to use terms in new ways that contradict common usage.

e.g. "A bachelor is (defined as) a human male who has never been married."

Logical: A logical statement is a statement whose truth can be known (tested) a priori, i.e., without recourse to observation of world states. e.g. "All bachelors are unmarried."

It would be a contradiction to deny the above statement. Such a contradiction would be a priori false. e.g. "Some bachelors are married," is a priori false.

(Don't confuse a so-called "bachelor" with bachelor as defined above. A "bachelor" is a human male who says he is not married. Some so-called "bachelors" may indeed be married.)

Empirical: An empirical statement is one whose truth can only be known (tested) a posteriori, i.e., by means of observations of the world. It is not a contradiction to deny an empirical statement. e.g., "Some bachelors are happy."

Given an appropriate definition of happy (e.g. report that they are happy), the above is probably a posteriori true. The statement, "All bachelors are happy" is probably a posteriori false.

Empirical Meaning: The empirical meaning of a sentence is equivalent to the set of testable, specifiable, measurable implications of the sentence. This definition of meaning is sometimes called "operationism" because the meaning of a sentence is said to be equivalent to the set of specifiable operations that one uses to test the sentence.

If "happiness" were defined as something inside someone's mind, then it becomes meaningless. If instead, we define happiness in terms of the behavior of a person (the person smiles, says that he or she is happy, etc.), then such statements are meaningful.

- Logically possible: If an empirical statement is not a contradiction, it is logically possible. e.g. "I can fly to the moon and back without a spaceship in .02 seconds."
- Logically impossible: A contradiction of definition and meaning. It is not logically possible for a bachelor to be married. It is logically possible for a bachelor to fly faster than the speed of light.
- Empirically possible: Consistent with the laws of nature (whatever they may be). We believe it is empirically possible to fly at a velocity of 1,000 miles/hour but not at a velocity of 10,000,000 miles per sec. It is not always obvious what is empirically impossible. Opinions or beliefs about empirical possibility change over time.
- Empirically impossible: Contradicts the laws of nature. We think it is empirically impossible to transport a human to the sun and back in less than .01 sec without a spaceship.
- Technically possible: A possibility that can now be achieved given the current state of technology. It was once technically impossible to fly to the moon, but it became technically possible in the 1960s. We assume it has always been empirically possible. Technically impossible: It is now assumed to be technically impossible for a human to live more than 150 years. (No one has done it).

Meaningful vs. meaningless statements

A meaningful statement can, in principle, be tested by operations that can be specified. The meaning of an empirical statement is equivalent to the set of implications for tests of its truth status by means of specifiable operations. If a statement has no implications (i.e., there are no tests or observations to make that might in principle refute the statement), then it is meaningless.

e.g., "On the far side of the moon there is a 7-up bottle cap."

Even though we cannot easily test this statement, it is logically possible to do so. We can imagine, for example, traveling to the moon and looking for the bottle cap. We understand the outcomes (finding it or not).

However, consider the following:

e.g., "Jack perceives red colors in his mind the way Jill perceives green, but both have learned the appropriate names to call them."

By definition, the contents of minds are considered private; that is, they are assumed to be logically impossible to observe. Therefore, it would be a contradiction to claim to observe Jack's or Jill's mind and thus the statement has no empirical implications and is thereby meaningless. It does have a certain poetic meaning.

Induction and Deduction

Deduction is an argument based on logical derivation of conclusions from premises. e.g. (P1) Socrates is an Athenian.

- (P2) All Athenians are Greek
- ∴ (C) Socrates is a Greek.

If the premises are true (and one shouldn't need to add--the deduction is logical--true deduction is always logical) then the conclusion is true. If the conclusion is false, then the premises have a problem. If the premises are false, the conclusion may or may not be false. If the conclusion is true, the premises may or may not be true.

- <u>Induction</u>: An inductive argument is used to establish an empirical generalization (such as a correlational or causal statement). The argument is based on the assumption that instances obtained at one time are samples of a population of instances that includes past and future events. The principle of induction asserts that if the proposition, λ :AB, has successfully been tested on n occasions, the credibility that λ will hold an occasion n + 1 is increased as n increases.
- Note: (Empirical induction should not be confused with mathematical induction which is actually a type of deduction).

e.g. λ : If you drop a pen near the surface of the Earth (A), it falls (B).

The association A_iB_i has held on over 1000 tests. To date, A with not B has never occurred. Therefore, if we drop a pen tomorrow, it seems believable that it too will fall.

Causation vs. Correlation

- <u>Correlation</u> is a relationship between two events. A correlational proposition states that events co-occur. If A and B are correlated, one can be used to predict the other. By induction, it may be argued that events shown to co-occur in the past will also co-occur in the future, a correlational generalization.
- e.g. The death rate due to starvation in India is correlated with the number of ice cream cones sold in New York City. The number of traffic accidents in a city is correlated with the number of telephones in the city.

Yearly economic indicators are correlated with the average length of women's skirts.

Evidence for a correlation statement should not be used as evidence for causation. Remember, correlation is the tool of the Devil!! Correlations are useful for prediction, but not for testing causation.

<u>Causation</u>: The statement A causes B implies that if A is caused to occur independently of other factors, then B will occur. If A_1 causes B and A_2 causes B, then A_1 and A_2 are said to be "sufficient" for the occurrence of B. If A_1 and A_2 are required for the occurrence of B and if it can be shown that without A_1 , then B will not occur, then A_1 is said to be "necessary" for the occurrence of B.

Causal statements are tested by experiments in which the suspected cause (A) is manipulated so as to make it independent of all other factors (this is often done by using a random process to control A or not A). The <u>independent variable</u> (e.g. A vs. not A) is manipulated and the occurrence of the suspected effect B (the dependent variable) is measured.

e.q. The Cambridge-Somerville Youth Study investigated whether psychotherapy caused a reduction in the probability of being convicted of crimes. Six hundred boys who had been identified as potential delinquents were randomly assigned to one of two groups by the toss of a coin. The treatment group received counseling and psychotherapy. The control group did not receive treatment. An equal proportion of boys were convicted of crimes. Boys in the treatment group actually were more likely to commit two or more crimes, and the probability of obtaining a difference this large by random assignment, given the null hypothesis of no difference, was less than .05. McCord (American Psychologist, 1978) in a thirty-year follow-up of the two groups concluded that the evidence indicated that psychotherapy was harmful, according to seven criteria of harm (age of death, criminal convictions, disease, alcoholism, occupational status, mental illness, and job satisfaction). In this example, treatment vs. no treatment was the independent variable, and there were many dependent variables

including criminal convictions, age at death, signs of alcoholism, signs of mental illness, blood pressure/heart trouble, prestige of occupations, and rated satisfaction of work.

Homework on Philosophical Terms

(Study definitions of Philosophical Terms; Study lecture notes and Ch 1-2 of by Kalat. Huff's book has examples of causation vs. correlation, discussed in chapter 8 titled "Post hoc rides again.") Define and give original examples of the following concepts: definition operational definition logical statement a priori true a priori false empirical statement a posteriori true a posteriori false meaningless sentence that sounds like an empirical statement induction deduction correlation statement evidence for correlation causal statement evidence of causation

Study ideas: After you have written your own examples, get together with a classmate or two and discuss your examples. Be sure to give clear definitions; otherwise your examples may be unclear.

Thought questions for this segment of the course:

- 1. What is the status of Freud's psychoanalysis as a theory? Does it satisfy the philosophical criteria of a theory?
- A. What are the major types of biological psychotherapies? B. What are the major types of "psychological" therapies?
- 3. How would you evaluate a new type of psychotherapy?
- 4. Is there any proof that any type of psychotherapy is beneficial?
- 5. What is the Barnum effect?
- 6. How are mental illnesses like medical illnesses? How are they different?

7. How accurate are clinical predictions of behavior? To learn more: Any book on Introduction to Philosophy should have sections on the topics of definition, meaning, causation and correlation. For example: Hospers, J. (1953). <u>An introduction to philosophical analysis</u>. Englewood Cliffs, NJ: Prentice-Hall, Inc.

Statistics Formulae

Score on Variable X for case \underline{i} : X_i Mode = Value of X that is most frequent Median = Value of X for which 50% of the cases are smaller Midpoint = $(X_{MAX} + X_{MIN})/2$ Range = $X_{MAX} - X_{MIN}$

Mean of Variable X, based on n cases:

$$\overline{X} = \frac{\sum_{i=1}^{n} X_i}{n}$$

 $s_X^2 = \frac{\sum_{i=1}^n (X_i - \overline{X})^2}{n}$

$$z_{X_i} = \frac{X_i - \overline{X}}{s_X}$$

 $s_x = \sqrt{s_x^2}$

Areas under Normal Distribution:

Standard Normal Distribution



Area from -1 to 1: .68 Area from -2 to 2: .95

Correlation Coefficient between X and Y: $r_{XY} = \frac{\sum_{i=1}^{n} z_{X_i} z_{Y_i}}{n}$

Predictions of Y from X and X from Y: Regression Equations:

- Y from X: $\hat{z}_{Y_i} = r_{XY} z_{X_i}$
- X from Y: $\hat{z}_{X_i} = r_{XY} z_{Y_i}$

The z-score of the predicted value is defined as:

$$\hat{z}_{Y_i} = \frac{\widehat{Y}_i - \overline{Y}}{s_Y}$$

Note that correlation coefficient is the slope of the regression (prediction) equation on the $z_{\mathbf{Y}}$ vs. $z_{\mathbf{X}}$ plot:



Errors (Residuals) of Prediction: residual = $Y_i - \hat{Y}_i$ score = predicted + residual (error) $Y_i = \hat{Y}_i + (Y_i - \hat{Y}_i)$

Total Variance = Variance Predicted + Variance of Residuals

 $s_Y^2 = r_{XY}^2 s_Y^2 + (1 - r_{XY}^2) s_Y^2$ Proportions: $r_{XY}^2 = r_{XY}^2 s_Y^2 + (1 - r_{XY}^2) s_Y^2$ That is, the average squared error (predicting Y from X): $\sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2$

$$s_{Y-\hat{Y}}^{2} = \frac{\sum_{i=1}^{N} (Y_{i} - Y_{i})^{2}}{n} = (1 - r_{XY}^{2})s_{Y}^{2}$$

Standard deviation of residuals (errors predicting Y from X):

$$\mathbf{s}_{\mathbf{Y}-\mathbf{Y}} = \sqrt{(1 - \mathbf{r}_{\mathbf{X}\mathbf{Y}}^2)\mathbf{s}_{\mathbf{Y}}^2}$$

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Statistics, IQ, and Personality Testing Homework

Be sure to study chapters in Kalat covering IQ, statistics, and personality testing, Huff's book, and class notes. Do #22 first (memorize the equations), then do items in order. See what you can do without looking at notes. Then study notes and books again, and try again.

- 1. Draw a frequency distribution of these 11 numbers: 0, 0, 1, 1, 5, 6, 7, 0, 9, 10, 30
- 2. Find the mean, median, mode, and midpoint of the numbers in No. 1.
- 3. What is the shape of the distribution in No. 1? Is it symmetric or asymmetric? Is it skewed? If it is skewed, is it positively or negatively skewed.
- 4. Find the mean, variance, and standard deviation of the following numbers: 10, 20, 30, 40, 30, 20, 50, 30, 30, 20, 40, 30, 40, 30.
- 5. Draw a frequency distribution for the numbers in No. 4.
- 6. Describe the shape of the distribution in No. 4-5. Find the median, mode, midpoint, and range.
- 7. Find the z-score of each value in No. 4.
- 8. Suppose a job placement test is normally distributed with a mean of 50 and a standard deviation of 15.
 - a. What percent of applicants who take the test scored below 80?
 - b. What percent scored between 50 and 80?
 - c. What percent score below 40? (Hint: if you can't find the answer exactly, approximate).
 - d. Suppose you need to be in the top 25% to be hired. What score do you need?

 z_{X_i} z_{Y_i} $z_{X_i}z_{Y_i}$

9. Here are some data from a study of the reliability of a projective test. The test was given twice to 14 patients, once each by two different clinical psychologists. The test is supposed to measure degree of neurosis. X = the first test score, Y = the second score. Compute the correlation coefficient between X and Y. Hint: both means are 30, both standard deviations are 10.

$X_1 = 30$	$Y_1 = 10$
$X_2 = 30$	$Y_2 = 50$
$X_3 = 10$	$Y_3 = 30$
$X_4 = 50$	$Y_4 = 30$
$X_5 = 30$	$Y_5 = 20$
$X_6 = 30$	$Y_6 = 40$
$X_7 = 20$	$Y_7 = 30$
$X_8 = 40$	$Y_8 = 30$
$X_9 = 30$	$Y_9 = 20$
$X_{10} = 30$	$Y_{10} = 40$
$X_{11} = 20$	$Y_{11} = 30$
$X_{12} = 40$	$Y_{12} = 40$
$X_{13} = 20$	$Y_{13} = 20$
$X_{14} = 40$	$Y_{14} = 30$

- 10. Draw a correlation scatterplot for the data in No. 9. Look again at Kalat's example scatterplots of correlations.
- 11. Is the test reliable? Discuss.
- 12. Is the test valid? Discuss. Should these scores be admitted as evidence in court?
- 13. Should this test be used to measure the outcome of a therapy experiment? Discuss.

- 14. Suppose the correlation between parent and child's IQ is .50. Suppose both IQ distributions are normal with means of 100 and standard deviations of 15.
 - a. Predict the child's IQ if the parent's IQ = 70.
 - b. Predict the child's IQ if the parent's IQ = 85.
 - c. Predict the child's IQ if the parent's IQ = 100.
 - d. Predict the child's IQ if the parent's IQ = 115.
 - e. Predict the child's IQ if the parent's IQ = 130.
- 15. Predict the parent's IQ if the child's IQ = 130.
- 16. Keeping the same assumptions as above, find the distribution of children's IQs for parents with IQs of 70, 85, 100, 115, and 130. Assume joint distributions are bivariate normal.
 - a. For each type of parent, estimate the probability that a child will have a higher IQ than the parent.
 - b. For each type of parent, find the probability that a child will have IQ > 100.
 - c. Suppose the correlation between IQs of husbands and wives is .6. Work out the distribution of the IQs of the husbands of women whose IQs = 130. Why do bright women rarely have husbands as smart as they are?
- 17. Suppose the correlation between IQ at age 8 and IQ at age 12 is 2/3, the correlation between ages 12 and 16 is also 2/3, and the correlation between IQs at ages 8 and 16 is 1/3. Hint: it will help to keep these correlation coefficients as fractions, rather than convert them to decimal equivalents.
 - a. Suppose we pick children who at age 8 have IQs of 70. Predict their average IQ at age 12 and at age 16.
 - b. Suppose we pick children at age 8 whose IQs are 130. Predict their mean IQs at age 12 and 16.
 - c. What do the results of *a* and *b* above suggest for before-after studies of remedial teaching or studies of gifted programs?
 - d. Suppose we pick children at age 16 whose IQs = 70. What were their mean IQs at ages 8 and 12?
 - e. Suppose we pick children at age 16 whose IQs = 130. What were their mean IQs at ages 8 and 12?
 - f. What do the results of *d* and *e* tell us about retrospective studies of gifted or retarded people? How does this statistical issue relate to the discussion of gifted people in the text?

- 18. Discuss the following issues concerning the IQ test.
 - a. What is the relationship between mental age and IQ for children? Why isn't chronological age used to define IQ for adults?
 - b. What is the reliability of the test? How is it measured? What is the typical value of the reliability coefficient?
 - c. What is the validity of the test? How is it measured? What are the typical results. Cite evidence.
 - d. What biases exist in the test? Cite evidence (not theory) for bias.
- 19. Complete the following table. Be sure to study the appropriate sections in the textbooks.

What are the actual correlation coefficients in IQ, according to empirical studies?

- a. Test-retest
- b. Alternate forms reliability
- c. IQ with SAT
- d. Husband's IQ by wife's IQ
- e. Parent-child, reared apart
- f. Parent-child, reared together
- g. Unrelated, reared apart
- h. Unrelated, reared together
- i. DZ (fraternal) twins, reared together
- j. DZ (fraternal) twins, reared apart
- k. siblings, reared together or apart
- 1. MZ twins, reared together
- m. MZ twins, reared apart
- 20. Describe the evidence concerning the heredity-environment debate. Are IQ scores determined mostly by heredity or environment? Cite evidence, not theory. Be sure to cite adoption studies, environmental intervention studies, and twin studies.
- 21. Compare the reliability and validity of the IQ test with those of the Projective tests, the MMPI, and personality tests like the CPI. Discuss the Barnum effect and the results of the clinical vs. statistical prediction literature.
- 22. Make sure you know the definitions and formulas for the following by heart.
 - a. Mean, Median, Mode, Midpoint
 - b. Shapes of distributions positive and negative skews, symmetric
 - c. Variance and standard deviation
 - e. Standard score (z-score)
 - f. Normal distribution (Areas: -2, -1, 0, 1, 2)
 - g. Correlation coefficient
 - h. regression-prediction equation
 - i. error of regression
 - j. reliability, validity
 - k. definition of test bias
 - 1. IQ = 100 MA/CA